**Average conditions for permanence in nonautonomous competitive systems with nonlocal dispersal**

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In this talk we consider the nonlinear evolution system.

$$\frac{\partial u_i}{\partial t} = \rho_i \left( \int_\Omega K_i(x,y) u_i(t,y) dy - u_i(t,x) \right) + f_i(t,x,u_1 \dots, u_N) u_i,$$
$$t \geq 0,\ x \in \bar{\Omega},\ i = 1, \dots, N,$$

where $u_i(t,x)$ is the density of the $i$th species at time $t$ and spatial location $x \in \bar{\Omega}$ and $\Omega$ is a compact spatial region, $\rho_i > 0$ is the dispersal rate of the $i$th species, $f_i(t,x,u_1,\dots,u_N)$ is the local per capita growth rate of the $i$th species and $K_i(\cdot,\cdot)$ is a nonlocal convolution kernel satisfying the following assumption: $K_i(\cdot,\cdot) : \bar{\Omega} \times \bar{\Omega} \to R$ are positive, $C^1$- functions such that $\int_\Omega K_i(x,y) dy = 1$ for any $x \in \bar{\Omega}$, $i = 1, \dots, N$. Applying Ahmad and Lazers definitions of lower and upper averages of a function and using the sub- and supersolution methods for PDEs we give sufficient conditions for permanence in such models. Moreover we allow the intrinsic growth rates to be negative.